The Scotsman Hotel, Edinburgh

Longevity risk: a pension-scheme perspective

Stephen Richards 10th October 2012



Copyright (c) Longevitas Ltd. All rights reserved. Electronic versions of related papers and presentations can be found at www.longevitas.co.uk

Contents

- 1. About the speaker
- 2. Enhanced annuities
- 3. Individual risk
- 4. Trend risk
- 5. Model risk
- 6. Conclusions

1. About the speaker

1. About the speaker

- Consultant on longevity risk since 2005.
- Founded longevity-related analytics businesses in 2006:



mortalityrating.com

• Joint venture with Heriot-Watt in 2009:



• Should a scheme buy enhanced annuities for members in ill health?

- Enhanced annuities give better rates for lives with shorter life expectancy.
- This market works well for individuals.
- Some companies market this as a way of reducing scheme liabilities.
- Unfortunately, this is often an illusion...

- Consider a scheme of ten male lives aged 65.
- \bullet Mortality follows 100% of S1PA in aggregate.
- Scheme reserve is $\pounds 671,000^{\dagger}$, i.e. $\pounds 67,100$ for each life on average.

 $\dagger \pounds_{5,000}$ pension p.a., paid continuously and discounted at 3% p.a. No mortality improvements.

- \bullet Assume that nine lives are healthy and follow 90% of S1PA.
- The tenth life is unhealthy and follows 262% of $S1PA^{\dagger}$.
- An enhanced annuity is purchased for the unhealthy life for $\pounds 47,200$.

[†]Life expectancy at 90% of S1PA is 18.9 years, while at 262% of S1PA it is 11.6 years.

• Superficially, the scheme appears to have saved nearly twenty thousand pounds on this one member ($\pounds 19,900 = \pounds 67,100 - \pounds 47,200$).

• This appears to save around 3% of scheme liabilities (3.0% = £19,900 / £671,000).

- The "saving" is an illusion.
- The remaining nine members are healthier than the old basis.
- Aggregate mortality is now 90% of S1PA, not 100%.
- The reserve for each of the remaining nine members therefore climbs from $\pounds 67,100$ to $\pounds 69,300$.
- The scheme reserve is now around $\pounds 623,700 \ (=9 \times \pounds 69,300)$.
- The difference between this and the starting reserve is $\pounds 47,300$, i.e. essentially the premium paid to the life insurer.

• If both the insurer and the pension scheme are properly reserving, there is negligible benefit from selectively buying out ill-health lives.

- The scheme is under-reserved if it doesn't strengthen its basis after such an exercise.
- Also, the mere fact that a scheme has conducted such an exercise can result in buy-out providers refusing to quote.

3. Individual risk

3. Individual risk

- What proportion of scheme liabilities are in a small number of hands?
- How does this drive risk?
- Should a scheme buy annuities for members with large benefits?

3. Concentration of risk

	Number of	Members with half
Scheme	Members	of total pension
Ε	38	4
Η	790	98
С	$5,\!272$	328

Largest scheme (C) pays 50% of all pensions to just 6% of members.

Source: Richards Consulting calculations using Prudential data.

Slide 14

3. Individual risk

- What impact does concentration have on scheme risk?
- What risk is posed from who dies when?
- What margin should be held to be confident of paying all benefits?

Safety $premium^*$			
Scheme	75%	90%	
E	15.1%	36.7%	
Η	4.0%	8.3%	
\mathbf{C}	2.1%	4.1%	

Law of large numbers favours schemes with more members.

Source: Richards Consulting calculations using Prudential data.

*Safety premium is the extra funds above average in 10,000 simulations to ensure given probability of meeting all benefits in run-off according to S1PA without any future improvements. Benefit cashflows discounted at 3% per annum.

Slide 16

3. Individual risk

- Small pension schemes should buy out.
- Bigger schemes can reduce risk by buying out members with large benefits.
- \bullet For example, Scheme H's 90% safety premium would fall from 8.3% to 4.4% if benefits were all equal.

4. Trend risk

4. Trend risk

• How much should a scheme reserve for trend risk?

4. Trend risk

- At the risk of stating the obvious, the future is unknown.
- This applies as much to mortality rates as to the level of the FTSE-100.

4. Mortality projections in the 20th Century

- Historically actuaries relied on deterministic scenarios.
- Often rates or improvements blending to a long-term value.
- Such models are called *expectations*.
- Cannot say how likely or unlikely such scenarios are.
- The CMI model is expectation-driven.

4. Mortality projections in the 21st Century

- Measuring uncertainty is now a key part of insurer regulations.
- A stress test ideally has a probability attached to it.
- Such tests and probabilities come from *stochastic projections*.

4. An illustration — back-testing

- Take a long data series.
- Discard latter years and fit projection model.
- Compare projected rates with what actually happened.

More on back-testing can be found on our blog

4. Back-testing: fit model to data to 1992



Source: Longevitas Ltd. ONS data, CMIR17

Slide 24

4. Back-testing: compare projections to actual data



Source: Longevitas Ltd. ONS data, CMIR17

Slide 25

4. Back-testing: data v. confidence intervals



Source: Longevitas Ltd. ONS data, CMIR17

Slide 26

5. Model risk

Slide 27

5. Model risk

- Confidence intervals show uncertainty about central projection
- What about uncertainty over the model?
- What if the projection model is not the right one?

5. Similar projections, different uncertainty



Source: Richards and Currie (2009), Figure 6

Slide 29

5. Different projections and intervals



Source: Richards and Currie (2009), Figure 5

Slide 30

6. Conclusions

- Buying enhanced annuities often doesn't help scheme finances.
- However, buying out large benefits *can* reduce risk.
- Stochastic models tell you about the impact of uncertainty.
- Never rely on just one projection model!



References

CMIB (CONTINUOUS MORTALITY INVESTIGATION BUREAU) **1999** *Report Number 17*, Institute and Faculty of Actuaries RICHARDS, S. J. AND CURRIE, I. D. **2009** *Assessing longevity risk and annuity pricing with the Lee-Carter model*, Faculty of Actuaries Sessional Meeting Paper, February 2009 RICHARDS, S. J. **2011** *Too good to be true?*, Longevitas Ltd

